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1 # Python code to solve problem with two knapsack-like constraints
2 #   by dynamic programming
3
4 # Helper functions for readability
5 # Weight is the first element of each state, volume is the second
6 def weight(i) :
7     return i[0]
8 def volume(i) :
9     return i[1]
10
11 hugeNumber = float("inf")
12
13 items = 4
14 weightCapacity = 300
15 volumeCapacity = 200
16 itemBenefit = ['unused', 800, 150, 300, 500]
17 itemWeight = ['unused', 40, 8, 20, 15]
18 itemVolume = ['unused', 10, 12, 22, 5]
19 numAvailable = ['unused', 3, 10, 4, 5]
20 stages = items
21
22 f = [dict( ) for t in range(stages + 2)]
23 x = [dict( ) for t in range(stages + 1)]
24
25 initialState = (weightCapacity, volumeCapacity)
26
27 # New component: reachable[t] is the set of states reachable in stage t
28
29 reachable = [set() for t in range(stages+2)]
30 reachable[1].add(initialState)
31 for t in range(1, stages+1) :
32     for i in reachable[t] :
33         maxCanInsert = min(numAvailable[t],
34                             int(weight(i)/itemWeight[t]),
35                             int(volume(i)/itemVolume[t]))
36         for d in range(maxCanInsert+1) :
37             reachable[t+1].add((weight(i)-d*itemWeight[t], volume(i)-d*itemVolume[t]))
38     print(str(len(reachable[t+1])) + " different states reachable at stage " +
39           str(t+1))
40
41 for i in reachable[stages + 1] :
42     f[stages+1][i] = 0
43
44 for t in range(stages, 0, -1) :
45
46     for i in reachable[t] :
47
48         maxCanInsert = min(numAvailable[t],
49                             int(weight(i)/itemWeight[t]),
50                             int(volume(i)/itemVolume[t]))
51         value = -hugeNumber
52
53         for d in range(maxCanInsert+1) :
54             j = (weight(i)-d*itemWeight[t], volume(i)-d*itemVolume[t])
55             moveValue = d*itemBenefit[t] + f[t+1][j]
56             if moveValue > value :
57                 value = moveValue
58                 bestMove = d
59

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60         # End of d loop
61
62         f[t][i] = value
63         x[t][i] = bestMove
64
65     # End of i loop
66
67 # End of t loop
68
69 print("Optimal value is " + str(f[1][initialState]))
70
71 solutionString = "Item counts :"
72 i = initialState
73 for t in range(1,stages+1) :
74     d = x[t][i]
75     solutionString += " " + str(d)
76     i = (weight(i)-d*itemWeight[t],volume(i)-d*itemVolume[t])
77
78 print(solutionString)
79 print("Total weight = " + str(weightCapacity - weight(i)) +
80       ", total volume = " + str(volumeCapacity - volume(i)))
81
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